

5
1 0
describe

apl utility programs

this workspace provides a collection of apl idioms and pseudo-primitives which are useful in a variety of application contexts.

apl idioms are single expressions which perform a single operation. they are most often used as a line, or part of a line, of an apl function. the function `<idioms>` in this workspace will list a collection of apl idioms which are separated into 8 categories.

apl pseudo-primitives are defined apl functions. their input comes from arguments, and their output is given through results returned. they are apl functions which can stand alone. they are usually either variants of existing apl primitives, or functions which work as complements to apl primitives.
the variable `<summary>` will list all of the pseudo-primitives which are collected in this workspace

idiomfns
package
idioms1

apl idioms -- structural

<code>((vector\vector)=\pvector)/vector</code>	• select unique elements
<code>(1,1\vector\=1\pvector)/vector</code>	• select unique elements from a sorted vector
<code>(1 1Q<\matrix\=Qmatrix)\+matrix</code>	• select unique rows
<code>(1,1\+\matrix\=1\pmatrix)\+matrix</code>	• select unique rows from a sorted matrix
<code>(1\=2\+\parray)\parray</code>	• make a row-oriented matrix
<code>(1\=2\+\parray)\parray</code>	• make a column-oriented matrix
<code>\((\pvector),1\pvector</code>	• make a 1 column matrix from a vector
<code>(1,\pvector)\pvector</code>	• make a 1 row matrix from a vector
<code>((0 1\+\pmat2)\+\pmat1)\+mat1,[1]</code>	• catenate 2 matrices along dimension 1
<code>((0 1\+\pmat1)\+\pmat2)\+mat2</code>	
<code>((1 0\+\pmat2)\+\pmat1)\+mat1,[2]</code>	• catenate 2 matrices along dimension 2
<code>((1 0\+\pmat1)\+\pmat2)\+mat2</code>	
<code>,vec1,[\]io+.5] vec2</code>	• interleave 2 vectors of same length

"\<,\> ", vector A enclose the vector individually
vector<'a b c'

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$$(z_0-1)+1+hi-z_0$$

9 integers between 10 and 11
limits

(vec1, vec2) [↑↑boot]

9 mesh 2 vectors according to
boolean vector

$x, [\Box \Diamond o - (\Diamond \Diamond p \wedge \Diamond \Diamond (p \Diamond x), \Diamond \Diamond y) / .5 \ 1] \ y$

9 catenate/laminate 2 arrays to form rows

$x, [\Box i o + (\neg \exists p \wedge /2 > (ppx), ppy) / .5 \ 1] \ y$

- catenate/laminate 2 arrays to form columns

(,b,[1.5] 1)/,b,[1.5] ~b

- generate expansion vector from boolean vector

idioms 2

api idioms -- sorting and searching

vector[Δ vector]

A sort a vector

```
matrix[ $\Delta(1+\rho \text{key}) \perp \!\!\! \perp \text{key} \mid \text{matrix};]$ 
```

9 sort the rows of a matrix

□ $i \otimes \text{matrix1} \wedge \text{matrix2} \neq \text{matrix1} \wedge \text{matrix2}$

first index of rows in a matrix

(vector=scalar)/vector

all indices of a scalar in a vector

L/vector elements

A first occurrence of several elements in a vector

(scalar×vector)×vector is scalar

(vector ≠ scalar) 11

```
vector[ $\Delta$ key]vector]
```

idioms3

apl idioms -- formatting

(+/^\! ' =array)Φarray	▫ left justify
(1-(array=' ')+1)Φarray	▫ right justify
width↑((L-/.5×width, 0text)○' '),text	▫ center
(\! ' ≠text)/text	▫ remove leading blanks
(Φ\! ' ≠Φtext)/text	▫ remove trailing blanks
((text≠' ')∨text≠1Φtext)/text	▫ remove duplicate, adjacent

5

blanks

((2*xptext)\\$1 0)\text

a double space text

idioms4
apl idioms -- predicates

0=\\$vector

a empty vector?

5

$0 \in \text{array}$ a empty array?
 $1 \in \text{array}$ a boolean array?
 $\text{array} = \text{array}$ a integer array?
 $0 = 1 \in \text{array}$ a numeric array?
 $\text{elements} \in \text{set}$ a all members of a set?
 $\text{elements} \in \text{set}$ a any members of a set?
 $\text{vector1} = \text{vector2}$ a 2 vectors identical?
 $\text{vector1}[\text{vector1}] \dots = \text{vector2}[\text{vector2}]$ a 2 vectors permutations of each other?
 $\text{axis} \in \text{array} = \text{axis} \in \text{array}$ a array in ascending order along certain dimension?
 $\text{axis} \in \text{array} = \text{axis} \in \text{array}$ a array in descending order along certain dimension?

idioms5

api idioms -- boolean shifts

$x \leftarrow 0\ 1\ 0\ 1\ 1\ 0\ 0\ 1\ 0\ 1\ 1\ 1\ 0\ 0\ 0\ 1$	
$x \wedge \neg 1 \downarrow 0, x$	$0\ 0\ 0\ 0\ 1\ 0\ 0\ 0\ 0\ 0\ 1\ 1\ 0\ 0\ 0\ 0$ a one and previous is one
$x \wedge \neg 1 \downarrow 1, x$	$0\ 1\ 0\ 1\ 0\ 0\ 0\ 1\ 0\ 1\ 0\ 0\ 0\ 0\ 0\ 1$ a one and previous is zero
$x \wedge 1 \downarrow x, 0$	$0\ 0\ 0\ 1\ 0\ 0\ 0\ 0\ 0\ 0\ 1\ 1\ 0\ 0\ 0\ 0$ a one and next is one
$x \wedge \sim 1 \downarrow x, 1$	$0\ 1\ 0\ 0\ 1\ 0\ 0\ 1\ 0\ 0\ 0\ 1\ 0\ 0\ 0\ 0$ a one and next is zero
$(\sim x) \wedge \neg 1 \downarrow 0, x$	$0\ 0\ 1\ 0\ 0\ 1\ 0\ 0\ 1\ 0\ 0\ 0\ 1\ 0\ 0\ 0$ a zero and previous is one
$\sim x \vee \neg 1 \downarrow 1, x$	$0\ 0\ 0\ 0\ 0\ 0\ 1\ 0\ 0\ 0\ 0\ 0\ 0\ 1\ 1\ 0$ a zero and previous is zero
$(\sim x) \wedge 1 \downarrow x, 0$	$1\ 0\ 1\ 0\ 0\ 0\ 1\ 0\ 1\ 0\ 0\ 0\ 0\ 0\ 1\ 0$ a zero and next is one
$\sim x \vee 1 \downarrow x, 1$	$0\ 0\ 0\ 0\ 0\ 1\ 0\ 0\ 0\ 0\ 0\ 0\ 0\ 1\ 1\ 0$ a zero and next is zero
$x \neq \neg 1 \downarrow (1 \uparrow x), x$	$0\ 1\ 1\ 1\ 0\ 1\ 0\ 1\ 1\ 1\ 0\ 0\ 1\ 0\ 0\ 1$ a previous bit is different
$x = \neg 1 \downarrow (\sim 1 \uparrow x), x$	$0\ 0\ 0\ 0\ 1\ 0\ 1\ 0\ 0\ 0\ 1\ 1\ 0\ 1\ 1\ 0$ a previous bit is same
$x \neq 1 \uparrow x, \neg 1 \uparrow x$	$1\ 1\ 1\ 0\ 1\ 0\ 1\ 1\ 1\ 0\ 0\ 1\ 0\ 0\ 1\ 0$ a next bit is different
$x = 1 \uparrow x, \sim \neg 1 \uparrow x$	$0\ 0\ 0\ 1\ 0\ 1\ 0\ 0\ 0\ 1\ 1\ 0\ 1\ 1\ 0\ 0$ a next bit is same

idioms6

apl idioms -- boolean scans

$x \leftarrow 1 1 1 0 1 1 0 1 0 0 0 1$
 $\wedge \backslash x \quad 1 1 1 0 0 0 0 0 0 0 0 0$ a ones until first zero from left

$x \leftarrow 1 1 1 0 1 1 0 1 0 0 0 1$
 $\sim \wedge \backslash x \quad 0 0 0 1 1 1 1 1 1 1 1 1$ a ones after first zero from left

$y \leftarrow 0 0 0 1 0 0 1 0 1 0 0 1$
 $\vee \backslash y \quad 0 0 0 1 1 1 1 1 1 1 1 1$ a zeros until first one from left

$y \leftarrow 0 0 0 1 0 0 1 0 1 0 0 1$
 $\sim \vee \backslash y \quad 1 1 1 0 0 0 0 0 0 0 0 0$ a zeros after first one from left

$z \leftarrow 0 0 1 1 1 0 0 1 0 0 1 0$
 $< \backslash z \quad 0 0 1 0 0 0 0 0 0 0 0 0$ a first one from left

$x \leftarrow 1 1 1 0 0 1 1 0 0 1 1 1$
 $\phi \wedge \backslash \phi x \quad 0 0 0 0 0 0 0 0 1 1 1$ a ones until first zero from right

$x \leftarrow 1 0 0 1 1 0 0 1 1 1 1 1$
 $\phi \sim \wedge \backslash \phi x \quad 1 1 1 1 1 1 0 0 0 0 0$ a ones after first zero from right

$y \leftarrow 1 1 0 0 1 0 1 0 0 0 0$
 $\phi \vee \backslash \phi y \quad 1 1 1 1 1 1 0 0 0 0 0$ a zeros until first one from right

$y \leftarrow 1 1 0 0 1 0 1 0 0 0 0$
 $\phi \sim \vee \backslash \phi y \quad 0 0 0 0 0 0 0 1 1 1 1$ a zeros after first one from right

$z \leftarrow 0 0 1 0 0 1 1 1 0 0 0 0$
 $\phi < \backslash \phi z \quad 0 0 0 0 0 0 1 0 0 0 0$ a first one from right

$v \leftarrow 0 1 0 0 0 1 0 0 1 0 1 0$
 $\neq \backslash v \quad 0 1 1 1 1 0 0 0 1 1 0 0$ a boolean finite state machine

$v \leftarrow 0 1 0 0 0 1 0 0 1 0 1 0$
 $v \vee \neq \backslash v \quad 0 1 1 1 1 1 0 0 1 1 1 0$ a ones and ones between ones

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$v \leftarrow 0 \ 1 \ 0 \ 0 \ 0 \ 1 \ 0 \ 0 \ 0 \ 1 \ 0 \ 1 \ 0$
 $(\sim v) \wedge \neq v \ 0 \ 0 \ 1 \ 1 \ 1 \ 0 \ 0 \ 0 \ 0 \ 1 \ 0 \ 0$ a ones between ones

idioms7

api idioms -- numerical

matrix×(ρmatrix)ρvector

a multiply vector times
rows of matrix

matrix×Q(Φmatrix)ρvector

a multiply vector times
columns of matrix

(+/[axis] matrix)÷(ρmatrix)[axis]

a average along specified
axis

array-0,[axis] (-axis=1)array↓array

a successive first differences
along specified axis

1|array

a fractional part of number

0 1Tarray

a split integer and fractional
part of numbers

1+Lbase@number

a number of digits needed to
represent number in base

(10*n)|number

a keep n digits from right

Lnumber÷10*n

a delete n digits from right

L.5+numbers

a round to nearest integer

(10*-n)×L.5+numbers×10*n

a round to n digits right
of decimal point

idioms8

api idioms -- object generators

 $(n, n) \circ 1, n \circ 0$

A identity matrix

 $(1^n) \circ . \geq 1^n$

A upper triangular matrix

 $(1^n) \circ . < 1^n$

A lower triangular matrix

integerΔvector $\circ . \geq 1^r /$ integerΔvector

A prefix 1's

integerΔvector $\circ . \geq \phi 1^r /$ integerΔvector

A suffix 1's

 $(2*n) \circ 0, 1^{-1+2*2*n}$ A truth table for n variables

summary

apl pseudo-primitives - variants and adjuncts to apl primitive functions

PRIMITIVE FUNCTION

FEATURE

+	Δ_{plus}	vector extension to rows and columns
-	Δ_{minus}	vector extension to rows and columns
\times	Δ_{times}	vector extension to rows and columns
\div	Δ_{div}	vector extension to rows and columns, commercial division
\lceil	Δ_{max}	vector extension to rows and columns
\lfloor	Δ_{min}	vector extension to rows and columns
/	Δ_{and}	vector extension to rows and columns

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v	Δor	vector extension to rows and columns
?!	Δperm	all permutations of m
?!	Δcomb	all combinations of m elements of n
[;]	Δmove	permutation with indexed fetch
[;]	Δfrom	matrix indexing
[;] ←	Δerplic	element replace by value
[;] ←	Δsrplic	string replace by value
o ⍳	Δmfv	matrix from vector, structure determined by value
o ⍳	Δvfm	vector from matrix, structure determined by value
o ⍳	Δreshape	generalized reshape by value
, ⍳	Δmat	make array into a matrix
, ⍳	Δjoin	extend catenate/laminate along [1]
, ⍳	Δlink	extend catenate/laminate along [2]
l ⍳	Δthru	integers between left and right argument
l ⍳	Δbetween	integers between pairs of integers
l ⍳	Δintegers	index generator for vectors
l ⍳	Δprogindex	progressive index lookup
l ⍳	Δlastindex	last index of
l ⍳	Δfind	string search- integer results
l ⍳	Δlocate	string search- boolean results
l ⍳	Δindexof	matrix first index of
∊ ⍳	Δmemberof	matrix member of
/	Δrepeat	replication with integer left argument
\	Δexpansion	generates argument for expand
↑	Δlff	negative overtake with left first fill
↑	Δrlf	positive overtake with right last fill
↑↓	Δtrim	take and drop based on values
↑	Δgradeup	grade up matrix

apl pseudo-primitives - variants and adjuncts to apl primitive and derived functions

PRIMITIVE FUNCTION

FEATURE

5

◊ m	Δpreverse	partitioned reverse
◊ a	Δrotate	partitioned rotate
◊	Δpgradeup	partitioned gradeup
◊	Δpgradedown	partitioned gradedown
/	Δpmask	creates boolean vector argument for /
+/	Δpplusreduce	partitioned plus reduce
+	Δpplusscan	partitioned plus scan
//	Δpanreduce	partitioned and reduce
/	Δpanscan	partitioned and scan
∨/	Δporreduce	partitioned or reduce
∨	Δporscan	partitioned or scan
Γ/	Δpmaxreduce	partitioned max reduce
Γ	Δpmaxscan	partitioned max scan
Λ/	Δpminreduce	partitioned min reduce
Λ	Δpminscan	partitioned min scan
=\	Δpeqscan	partitioned equal scan (boolean)
≠\	Δpneqscan	partitioned not equal scan (boolean)
<\	Δpltscan	partitioned less than scan (boolean)
≤\	Δpleqscan	partitioned less than or equal scan
‡	Δnums	convert characters to numbers
◊	Δformat	format numbers, fill overflows with *
◊	Δfmtblank	format numbers, blank out zeros
◊	Δfmtcommas	format numbers, insert commas
◊	Δfmtleft	format numbers, left justify
◊	Δfmtminus	format numbers, use middle minus
◊	Δfmtpic	format numbers using picture
◊	Δfmtsmall	format numbers into smallest space
◊	Δfmtzero	format numbers, zero fill